



**QUESTION 1**

**a**  $3 \cdot 34$

**b**  $(3x-2)(x-3)$

**c**  $1.5 \times 10^8$

**d**  $\frac{2x-5}{4} = 7-x$

$2x-5=28-4x$

$6x=33$

$x=5\frac{1}{2}$

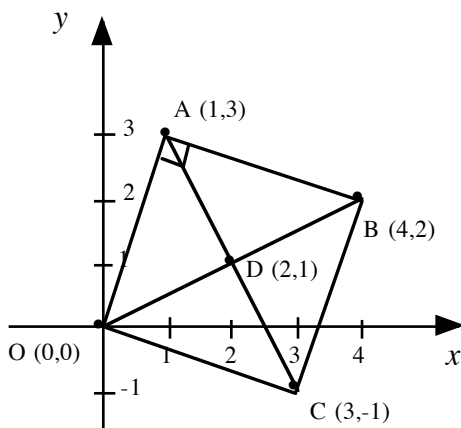
**e**  $T=2\pi\sqrt{\frac{L}{g}}$

$L=\frac{gT^2}{4\pi^2}$   $g=10$   
 $T=1.4$

$\approx 0.496\text{m}$

**QUESTION 2**

**a i**



**ii**  $m_1 = \text{Slope } OA = 3$

$m_2 = \text{Slope } OB = \frac{1}{2}$

**iii** Slope AB  $m_3 = -\frac{1}{3}$

since  $m_1 m_3 = 3 \times -\frac{1}{3} = -1$

then  $OA \perp AB$

**iv**  $OA = \sqrt{1^2 + 3^2}$   
 $= 10$

$AB = \sqrt{1^2 + 3^2}$   
 $= \sqrt{10}$

$\therefore OA = AB$

**v** Mid-pt of OB is  $D = (2,1)$

**vi**  $C = (3,-1)$

**vii** OABC is a square

**b** 12 males, 18 females. Pr (at least 1 male) =  $1 - \text{Pr (all females)}$

$\therefore \text{Pr (at least 1 male)} = 1 - \frac{18}{30} \times \frac{17}{29} \times \frac{16}{28}$

$= \frac{811}{1015} (\approx 0.7990)$

**QUESTION 3**

**a i**  $y = 2x^3 - 5x + \frac{3}{4x^3} - 7$

$y' = 6x^2 - 5 - \frac{9}{4x^4}$

**ii**  $y = 5(3x^2 - x)^7$

$y' = 35(3x^2 - x)^6 (6x - 1)$



iii  $y = x \sin 2x$

$$\frac{dy}{dx} = \sin 2x + 2x \cos 2x$$

iv  $y = \frac{x}{1+x}$

$$\frac{dy}{dx} = \frac{1}{(1+x)^2}$$

b i  $\int_0^1 e^{3x} dx = \frac{1}{3} e^{3x} \Big|_0^1$   
 $= \frac{1}{3}(e^3 - 1)$

ii  $\int_0^5 \sqrt{3x+1} \cdot dx = \frac{2}{9}(3x+1)^{3/2} \Big|_0^5$   
 $= \frac{2}{9}(64 - 1)$   
 $= 14$

#### QUESTION 4

a  $y = \ln(2+x^2)$  when  $x=2$ ,  $\frac{dy}{dx} = \frac{2}{3}$   
 $\frac{dy}{dx} = \frac{2x}{2+x^2}$

b  $\cot 330^\circ \cdot \sec 240^\circ = -\sqrt{3} \times -2$   
 $= 2\sqrt{3}$

c  $\cos C = \frac{4^2 + 5^2 - 7^2}{2 \times 4 \times 5} \therefore$  Largest angle  $= 101^\circ 32'$

d  $T_8 = a + 7d = 41 \therefore 6d = 18$

i  $T_2 = a + d = 23 \quad d = 3 \quad a = 20$

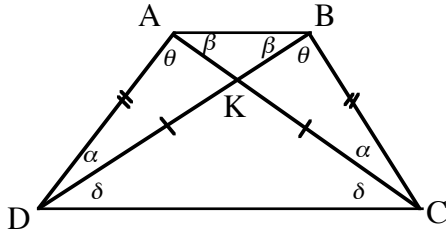
ii  $S_{50} = \frac{50}{2}(40 + 49 \times 3) = 4675$

#### QUESTION 5

a Michael investment  $= \frac{\$200 \left(1 + \frac{1}{240}\right) \cdot \left[\left(1 + \frac{1}{240}\right)^{12} - 1\right]}{\frac{1}{240}}$   
 $= \$2466.00$



**b i**



**ii** In  $\Delta$ 's ABD, ABC

$$AD = BC \text{ (data)}$$

$$BC = AC \text{ (data)}$$

$$AB = AB \text{ common side}$$

$$\therefore \Delta ABD \cong \Delta ABC \text{ (S.S.S.)}$$

$$\therefore \angle ADB = \angle BCA = \alpha \text{ (corresp angles in cong } \Delta \text{'s) and } \angle BAC = \angle ABD = \beta$$

$$\therefore \Delta AKB \text{ is isosceles with } AK = BK$$

$$\therefore \text{In } \Delta AKD, BKC$$

$$AK = BK \text{ proved} \quad ; \quad \angle ADK = \angle BCA = \alpha \text{ proved}$$

$$\angle AKD = \angle BKC \text{ (vert opp)} \quad \therefore \Delta AKD \cong \Delta BKC \text{ (A.A.S.)}$$

**iii**  $\therefore KC = KD$  (corresp sides in cong  $\Delta$ 's)

**iv**  $\angle ADC = \angle BCD$  ( $\Delta ADC \cong \Delta BCD$  S.S.S.)

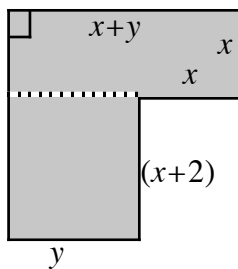
**v** Note:  $\Delta ABK \cong \Delta DKC$  (isos with vert  $\angle$ 's equal)  
 $\therefore \angle BAC = \angle BDC$  but these are alt  $\therefore AB \parallel DC$

**QUESTION 6**

**a i** Per =  $2(x+y) + 2(2x+2) = 48 + 2x$

$$\therefore y + 3x = 22 + x \text{ or } y = 22 - 2x$$

**ii** Shaded Area  $A(x) = x(x+y) + y(x+2)$



$$= x^2 + 2xy + 2y$$

$$= x^2 + (2x+2)(22-2x) - 3x^2 + 40x - 44$$

$$A(x) \text{ is a max when } A'(x) = 0 \text{ \& } A''(x) < 0$$

$$\therefore -6x + 40 = 0 \quad A''(x) = -6 < 0 \quad \therefore \text{max}$$

$$x = 6\frac{2}{3}$$

$$\therefore \text{Max Area when } x = 6\frac{2}{3} \text{m, } y = 8\frac{2}{3}$$

**QUESTION 6 (cont)**

**b**  $2x^2 + 3x - 4 = 0$  has roots  $\alpha, \beta$

**i**  $\alpha + \beta = -\frac{3}{2}, \alpha\beta = -2$

**ii**  $\alpha^2 + \beta^2 = (\alpha + \beta)^2 - 2\alpha\beta = 6\frac{1}{4}$

**c**  $x^2 - kx + 1 = 0$  Pos def  $\Delta < 0$  ie  $-2 < k < 2$



**QUESTION 7**

**a i**  $PA = \sqrt{(x+1)^2 + y^2}$        $PB = \sqrt{(x-2)^2 + y^2}$  ,  $PA = 2PB$

**ii**  $PA^2 = 4PB^2$      $(x+1)^2 + y^2 = 4(x-2)^2 + 4y^2$

$y^2 + x^2 - 6x + 5 = 0$     circle

**iii**  $(x-3)^2 + y^2 = 4$     circle (3,0); r=2

**b i**    Amt after Yr 1 =  $\$50000(1.08) - M$   
      Amt after Yr 2 =  $[\$50000(1.08) - M]1.08 - M$   
                          =  $\$50000(1.08)^2 - M(1 + (1.08))$

**ii**    Amt after 20th withdrawal  
 $0 = \$50000(1.08)^{20} - M(1 + (1.08) + \dots + (1.08)^{19})$

**iii**  $M = \frac{50000(1.08)^{20}}{(1.08)^{20} - 1} \times 0.08 \approx \$5092.61$

**iv**    Interest of 15% gives \$8000/Yr